

Number Pattern

$$1^3 + 5^3 + 3^3 = 153$$

$$16^3 + 50^3 + 33^3 = 165033$$

$$166^3 + 500^3 + 333^3 = 166500333$$

$$1666^3 + 5000^3 + 3333^3 = 166650003333$$

The number pattern can continue, can you prove this using algebra?

The proof is as follows:

$$\begin{aligned} & \left(\frac{10^n-4}{6}\right)^3 + \left(\frac{10^n}{2}\right)^3 + \left(\frac{10^n-1}{3}\right)^3 \\ &= \frac{1}{6^3} [(10^n - 4)^3 + 27(10^n)^3 + 8(10^n - 1)^3] \\ &= \frac{1}{6^3} \left[(10^{3n} - 12 \times 10^{2n} + 48 \times 10^n - 64) + 27 \times 10^{3n} \right. \\ & \quad \left. + (8 \times 10^{3n} - 24 \times 10^{2n} + 24 \times 10^n - 8) \right] \\ &= \frac{1}{6^3} [36 \times 10^{3n} - 36 \times 10^{2n} + 72 \times 10^n - 72] \\ &= \frac{1}{6} [10^{3n} - 10^{2n} + 2 \times 10^n - 2] \\ &= \frac{1}{6} (10^{3n} - 4 \times 10^{2n}) + 5 \times 10^{2n-1} + \frac{10^n-1}{3} \end{aligned}$$

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